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# THE G C SCHOOL OF CAREERS 

## ENTRANCE EXAMINATION

## SCHOOL YEAR 2021-2022

## MATHEMATICS

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## GOOD LUCK

Time: 1 hour and 30 minutes

## MATHEMATICS

- This paper consists of $\mathbf{2 5}$ questions.
- Answer ALL the questions in the space provided.
- Show all your workings.
- The use of a calculator is not allowed.
- Write your answers clearly.

1. Calculate the following and simplify your answer:
a) $\frac{1}{4}+\frac{3}{12}+\frac{4}{16}+\frac{5}{20} \times 5=$
(3)

Answer: $\qquad$
b) $\left(5 \frac{1}{9}+\frac{5}{12} \div \frac{3}{4}\right) \times 0.6+0.6=$
(4)

Answer: $\qquad$
c) $\frac{5+5 \times \frac{1}{5}-3^{2}+1^{5} \times 8}{\left(\frac{1}{2}\right)^{3}}=$

Answer:
2. Find the value of $a$ and $b$.

(2)

Answer: $\mathrm{a}=$ $\qquad$ , $b=$ $\qquad$
3. A container full of milk weighs 25 kg . The same container half-filled with milk weighs 13 kg . Find how much the empty container weighs.

Answer: $\qquad$
4. The teacher wrote on the board the smallest integer whose sum of digits is equal to 20 . Find the tens digit of this number.

Answer: $\qquad$
5. On a table there are triangles and quadrilaterals made of cardboard which have no contact with each other. We count a total of 27 peaks. If you know that there is more than one triangle, find how many triangles and how many quadrilaterals are on the table.

Answer: triangles $\qquad$ quadrilaterals $\qquad$
6. $A B C D$ is a square. The points $E$ and $Z$ are the midpoints of the sides $A B$ and $A D$ respectively. $M$ is the midpoint of the diagonal $B D$. Find what percentage of the area of the square is the area of the triangle EMB.


Answer: $\qquad$
7. John needs 16 minutes to read from the beginning of page 8 to the end of page 15 of a book. If he started on page 32 of the book at 5:07 p.m., find which page he will be reading at 5:55 p.m.

Answer: $\qquad$
8. George wants to buy basketballs. If he buys five basketballs, he will have $€ 20$ left in his wallet. If he buys seven basketballs, he will have to give $€ 16$ more than the money he has. How much does each basketball cost?
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9. An aquarium is full of water up to $\frac{11}{14}$ of its capacity. I want to decorate it, so I remove 126 litres of water. When I remove the water, the aquarium will be half full. Find how many litres of water the aquarium can hold when full.

Answer: $\qquad$

10. A four-digit number has the number 3 in the place of tens. The sum of the first three digits is 15 .

Find the missing digits of the number if you know that:

- the number is divisible by 3 but not 4 .
- if you write the digits in the reverse order, the new number is divisible by 5 .


11. On the line below, the length of $A B$ is the $\frac{1}{4}$ of the length of $A C$. Find which number corresponds to the letter $B$ and what the distance $B C$ is.
(4)

(Diagram not accurately drawn)

Answer: $\mathrm{B}=$ $\qquad$ , $B C=$ $\qquad$
12. George's mother bought 30 kilos of honey and 20 kilos of sugar from a food store. He paid a total of $€ 108$. If 3 kg of honey cost as much as 10 kg of sugar, how much does 1 kg of honey cost?
13. At a theater, the regular ticket costs $€ 4$ more than the children's ticket. We know that 4 regular tickets and 2 children's tickets cost $€ 64$. Find how much a regular ticket costs and how much a children's ticket costs.
(4)

Answer: Regular ticket $\qquad$ ,

Children's ticket $\qquad$
14. Nick buys tea at $€ 5$ per kilo ( Kg ) and sells it $€ 1.25$ per 200 grams (g). Find his percentage profit.

Answer: $\qquad$
15. The numbers $\alpha$ and $\beta$ verify the following equations.

Find the numbers $\alpha$ and $\beta$.

- $\frac{36}{\alpha}+7=10$
- $\alpha-\frac{\beta}{2}=15-\alpha$

Answer: $\alpha=$ $\qquad$ , $\beta=$ $\qquad$
16. In the figure below $A B C D$ and CDEZ are identical squares. $D$ and $C$ are the midpoints of sides $A E$ and $B Z$ respectively. $K$ and $M$ are random points on the sides $A B$ and $E Z$. If the perimeter of the rectangle $A B Z E$ is 48 cm , find the area of the shaded region.


Answer: $\qquad$
17. The pie chart below gives information about the expenditure of a gas company in one year.


## (Diagram not accurately drawn)

The amount spent on materials is 369 million euros. The amount spent on services is the same as the amount spent on wages.

Find the amount spent on services.

Answer: $\qquad$ million
18. In a class there is an equal number of boys and girls. Nine girls leave the classroom to take part in a show. Now the number of boys in the class is twice the number of girls. Find how many boys and girls in total had been in the class, before the 9 girls left.

Answer: $\qquad$
19. Inside a box I have several cards

3 black, 11 white, 9 blue and 7 red
Complete the following.
If I pick a card at random from the box:

- The probability of its colour being ___ is $\frac{3}{10}$.
- The probability that it is not blue in percentage is $\qquad$ .

If I add more black cards into the box and pick a card at random, the probability of it being black is $\frac{1}{4}$.

- How many black cards did I add in the box? $\qquad$

20. In the figure below $A E D$ is an equilateral triangle, $A B=B D$ and angle B is a right angle. Work out the size of angle $E A B$.

(Diagram not accurately drawn)

Answer: $E A B=$ $\qquad$
21. There are 150 balls in a box. $60 \%$ of the balls are black and the rest are white. We remove $15 \%$ of the white balls from the box and add 29 black balls. Find the ratio of white balls to the total number of balls in the box.
(5)

Answer: $\qquad$
22. A rabbit and the cage it is in, weigh 4.2 kg . A goose and its cage (identical to the rabbit's cage) weigh 5.2 kg . The goose and the rabbit together weigh 3.4 kg . Find the weight of the cage.

Answer:
23. The average of twelve numbers is 25 . If we delete two numbers, the average of the remaining numbers is 19 . Find the numbers we deleted if one number is three times the other one.

Answer:
24. In a piggy bank there are $18 € 1$ and $€ 2$ coins with a total weight of 143 grams. There is no other money in the piggy bank. Each €1 coin weighs 7.5 grams and each $€ 2$ coin weighs 8.5 grams. Find the total amount of money in the piggy bank.
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25. There are 120 rooms in a hotel. $60 \%$ of the rooms have air conditioning and the rest do not. Today $75 \%$ of the hotel rooms are occupied. $\frac{2}{3}$ of the occupied rooms have air conditioning. What percentage of rooms without air conditioning are available.
(5)

Answer: $\qquad$

END

